

Astronomy 102: Stars and Galaxies

Review Examination 1

Do not open the test until instructed to begin.

Instructions: Write your answers in the space provided. If you need additional space, continue on the back of each page, but indicate **clearly** that you have done so. No books, notes, or assistance from anyone is allowed. You are allowed to use, and will need, a calculator. Please **write legibly and be brief and to the point!** The exam has seven questions; each question has equal weight.

Possibly Useful Constants and Formulae

$$R_{\odot} = 6.96 \times 10^5 \text{ km}$$

$$M_{\odot} = 1.99 \times 10^{30} \text{ kg}$$

$$c = 3.00 \times 10^8 \text{ m s}^{-1}$$

$$1 \text{ pc} = 3.26 \text{ yr}$$

$$1 \text{ pc} = 206,265 \text{ AU}$$

$$1 \text{ AU} = 1.496 \times 10^{11} \text{ m}$$

$$1 \text{ km} = 1,000 \text{ m}$$

$$E = m c^2$$

$$eff = \frac{E_{\text{produced}}}{m c^2}$$

| Process | Efficiency |
|--------------------|-----------------|
| Chemical Reactions | $\sim 10^{-10}$ |
| Nuclear Reactions | $\sim 10^{-2}$ |
| Total Conversion | 1 |

Age of Solar System: 4.6×10^9 years

Age of Universe: 13.7×10^9 years

1. Some websites raise an objection to the scientific evidence for the age of the Solar System which goes as follows: Carbon dating is not effective at measuring ages of billions of years.
 - (a) Is this statement correct? Explain.
 - (b) Supposing this statement is correct (whether or not it is really correct), is this statement relevant to the scientific evidence for a 4.6 billion year old solar System? Explain.

2. You have a sample of a radioactive isotope with a half life of 30 minutes. You use a Geiger counter to measure the decay rate, and measure 20 decays per second.
 - (a) How many decays per second will you measure from this sample one hour from now?
 - (b) How long will you have to wait until you will hear no more clicks forevermore from the sample? Explain.
 - (c) After you've waited the first half-hour, you pick out a single isotope that has managed to survive through that first-half hour. What is the probability that this one isotope will decay in the *next* half-hour?

3. We have found rocks (meteorites) that have a Potassium-40/Argon-40 ratio of about 0.08, and from this have concluded that the Solar System is 4.6 billion years old. Suppose you find a rock that has a Potassium-40/Argon-40 ratio of 0.2. What, if anything, does this rock say about the age of the Solar System? (Give a qualitative answer; I don't expect hard numbers.) Explain your reasoning.

4. Later in the Sun's life, it will swell and become a Red Giant; it will be enough bigger that its luminosity (amount of energy generated each second) will have gone up by a factor of 100. The first part of the red giant phase of the Sun's life will last less than 10% of the phase we're currently in. During the first part of the red giant phase, the Sun will still be generating energy via Hydrogen fusion at its core.
 - (a) By $E = mc^2$, knowing that the Sun is right now using up some of its mass to generate energy, approximately what (to two significant figures) will be the Sun's mass at the *beginning* of this phase? (Ignore any mass loss due to the Solar Wind or other mass ejections.)
 - (b) Will the rate at which mass is converted to energy be *higher*, *the same*, or *lower* when the Sun is a red giant, as compared to now? Explain.
 - (c) How will the *eff* (efficiency) of the energy generation process during the first part of the Sun's red giant phase compare to the *eff* of the energy generation process in the Sun right now?